# **MATHEMATICS - CPA**

Across the Federation, we use a **CPA** (concrete, pictorial, abstract) approach to teach mathematical fluency.

Children are introduced to new mathematical concepts through the use of **concrete** objects (e.g. counters). They then explore concepts **pictorially** (usually representations of the concrete objects they have used) and finally, they solve problems where they only have the **abstract** (i.e. numbers and symbols). Building these steps helps children secure their understanding by seeing the relationship between numbers and the real world.

Concrete	Pictorial	Abstract		
		3 + 2 = 5		

Teachers will post their **Maths Working Walls** each week on Class Dojo. This will show what your child has learned in mathematics at school that week and will also show the strategies used to teach different mathematical concepts. Understandably, it is really important that the strategies used at home are the same as the strategies that we use in school.

Outlined on the pages that follow are some of the approaches and resources that we use to teach addition, subtraction, multiplication and division.

# **K\$1 ADDITION**

•	Concrete	Pictorial	Abstract		
Part Whole Models	6	6000	6 4 2 4 + 2 = 6		
Number lines	$\begin{array}{c c} \cdot & & \\ \bullet & 1 & 2 & 3 & 4 & 5 \\ \hline & & & & \\ \hline & & & & \\ \hline & & & & \\ \hline & & & &$	$\begin{array}{c} \bullet \\ \bullet \\ \circ \\ \circ \\ \bullet \\ \bullet \\ \bullet \\ \bullet \\ \bullet \\ \bullet \\$	$\begin{array}{c} \bullet \\ \bullet \\ 0 & 1 & 2 & 3 & 4 & 5 \\ \hline 1 & + & 3 & = & 4 \end{array}$		
Ten Frames			$ \begin{array}{c} 8 + 2 = 10 \\ 10 + 3 = 13 \\ 8 + 5 = 13 \end{array} $		
Base-ten blocks		00	30 + 4 = 34		
Place Value Counters			$\begin{array}{c} 20 + 30 = 50 \\ \hline 1 + 2 = 3 \\ \hline 50 + 3 = 53 \\ \hline 21 + 32 = 53 \end{array}$		

### **K\$1 SUBTRACTION**

$\overline{}$	Concrete	Pictorial	Abstract		
Numicon		00888	5 - 3 = 2		
Number lines	$\begin{array}{c} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$	$\begin{array}{c} \bullet \\ \bullet $	$\begin{array}{c} \bullet \\ \bullet \\ 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ - \\ 3 \\ - \\ 1 \\ \end{array}$		
Ten Frames			<u>12</u> – <u>3</u> = <u>9</u>		
Base-ten blocks	X	X X X X X X X X X X X X X X X X X X X	34) <b>-</b> 13) = 21)		
Place Value Counters			$ \begin{array}{c} 40 - 10 = 30 \\ 3 - 1 = 2 \\ 43 - 11 = 32 \end{array} $		

# **K\$1 MULTIPLICATION**

×	Concrete	Pictorial	Abstract		
Numicon		$ \begin{array}{c} \odot \odot \odot \odot \\ \odot \odot \odot \end{array} $	7 x 2 = 14		
Cubes	*** ** *** **		4 x 5 = 20		
Base-ten blocks			6 x 10 = 60		
Arrays		00000 00000 00000	3 x 5 = 15		

### **KS1 DIVISION**

$(\div)$	Concrete	Pictorial	Abstract
Sharing			6 ÷ 2 = 3
Grouping			20 ÷ 5 = 4
Arrays		0000000000 0000000000 0000000000 000000	(40) ÷ (10) = (4)

Capacity	<b>Capacity</b> The amount of space inside an object (the amount of liquid or air it contains).				
Difference	By how much a number is bigger or smaller than another (e.g. the difference between 4 and 6 is 2).				
Digit	<b>git</b> Any single number from 0 to 9 (inclusive).				
Edge	The intersection of two faces (the line along which they join) of a three-dimensional shape.				
Even number	A positive or negative number exactly divisible by 2.				
<b>Face</b> A plane (flat) surface of a three-dimensional object.					
<b>Greater than</b> The symbol used to represent greater than is an arrow pointitiowards the smallest number (e.g. 6 is greater than 2 is 6					
Hexagon	A polygon (2 d shape) with six sides.				
Half The part of a shape (or number) when divided exactly into parts.					
<b>Less than</b> The symbol used to represent less than is an arrow pointing towards the smallest number (e.g. I is smaller than 4 is 1					
Oblong	A shape with two pairs of straight, unequal sides and four right angles (also known as a rectangle).				
<b>Odd number</b> A number that when divided by two leaves a remainder of on					
Ordinal number	Describes a position in a number sequence.				
Place valueIndicates the value of a digit (the amount it is worth)e.g. the place value of the 3 in 32 is 30.					
<b>Sum</b> The result when two or more numbers are added together.					

Decrease	To make smaller (take away) or a pattern of numbers that is getting smaller.
Horizontal	Describes a line or plane parallel to the Earth's surface.
Irregular shapes	Shapes do not have sides of equal length or equal angles.
Increase	To make larger (add to) or a pattern of numbers that is getting larger.
Kite	A quadrilateral that has two adjacent pairs of sides that are equal in length, and at least one pair of opposite angles are equal.
Line of symmetry	A line that divides a shape into equal halves.
Multiple	The product of a given number with another factor.
Octagon	A polygon (2D shape) with eight sides and eight angles.
Regular shape	A shape with equal sides and angles.
Vertical	A line that is perpendicular (at a right angle to the horizontal).

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Acute	Describes angles between 0 and 90 degrees.
Alternate	Every other one in a sequence.
Angle	The number of degrees rotated around a point.
Ascending order	The arrangement of numbers from smallest to largest.
Axis of symmetry	A line dividing a shape into two symmetrical parts.
Base	The line or face on which a shape is standing.
Breadth	Another name for width - the distance across from side to side.
Denominator	The number below the line in a fraction.
Descending order	The arrangement of numbers from the largest to smallest.
Diagonal	A straight line connecting 2 non-adjacent vertices of a polygon.
Dimensions	The measurements of a shape (i.e. length, width, height).
Heptagon	A 2D shape, also called a septagon, with 7 sides and 7 angles.
Interior	Another word for 'inside'.
Isosceles triangle	A triangle which has two sides of equal length.
Numerator	The number above the line in a fraction.
Obtuse angle	An angle between 90 and 180 degrees.
Parallelogram	Quadrilateral with 2 pairs of parallel lines & equal opposite angles.
Perimeter	The length of the distance around the boundary of a shape.
Perpendicular line	A line at right angles to another line or plane.
Product	The result when two or more numbers are multiplied.
Quadrilateral	A four sided shape.
Quarter	A shape or number divided in to 4 equal parts.
Rhombus	A parallelogram with congruent (equal) sides. Opposite sides are parallel and opposite angles are equal in size.
Roman numerals	Seven letters are used in combination to write numbers: $\mathbf{I} = 1, \ \mathbf{V} = 5, \ \mathbf{X} = 10, \ \mathbf{L} = 50, \ \mathbf{C} = 100, \ \mathbf{D} = 500 \ \& \ \mathbf{M} = 1000$
Rounding	An approximation used to express a number more conveniently.
Scale	A series of regular marks along a line used to measure or count.
Trapezium	A quadrilateral with two parallel sides.

Area	The amount of space within a perimeter (expressed in square units).
Coordinates	Numbers used to locate a point on a grid.
Equilateral triangle	A triangle with equal angles and equal sides.
Factor	A number which will divide exactly into another number.
Isosceles triangle	A triangle with two equal sides and two equal angles.
Improper fraction	A fraction with a numerator greater than its denominator.
Quadrant	A quarter of the area of a circle, containing a right angle.
Scalene triangle	A triangle with three unequal side lengths and no equal angles.
Translation	When a shape is moved from one place to another just by sliding it (without rotating, reflecting or enlarging).

Adjacent	Adjoining (as used to describe lines and angles).
Average	A number representing a set of numbers (obtained by dividing the total of the numbers by the numbers itself).
Carroll Diagram	A problem-solving diagram used in classification activities.
Composite number	A number with more than two factors.
Integer	A negative or positive whole number.
Polyhedron	A three dimensional shape with plane faces.
Prime number	A number with only 1 and itself as factors (e.g. 2, 3, 5, 7,11 etc.).
Quotient	The result when one number is divided by another number.
Reflex angle	An angle greater than 180 degrees.
Rotational symmetry	A shape is said to have rotational symmetry if it looks the same in different positions when rotated about its centre.
Squared	A number squared is a number multiplied by itself.
Square number	A number whose units can be arranged into a square (e.g. 1, 4, 9, 16, 25, 36, 49, 64 etc.).

Algebra	Algebra Letters are used to represent numbers and quantities.					
Bisect	To divide into two equal parts.					
Circumference	The distance around a circle (its perimeter).					
Congruent	Congruent shapes are the same shape and size					
Dodecagon	A twelve sided polygon.					
Equation	A statement of equality between two expressions (e.g. $3 \times 4 = 6 + 6$ ).					
Mean	The average of a set of numbers. The sum of the values in a set of data divided by the total number of items in that set.					
Tessellation	Shapes fitted together with a number of exact copies and with no overlaps or gaps.					
Triangular number	A number whose units can be arranged into a triangle (e.g. 1, 3, 6, 10, 15, 21)					

#### **MATHEMATICS TABLES – PART 1**

x	1	2	3	4	5	6	7	8	٩	10	11	12
1	1	2	3	4	5	6	7	8	q	10	11	12
2	2	4	6	8	10	12	14	16	18	20	22	24
3	3	6	٩	12	15	18	21	24	27	30	33	36
4	4	8	12	16	20	24	28	32	36	40	44	48
5	5	10	15	20	25	30	35	40	45	50	55	60
6	6	12	18	24	30	36	42	48	54	60	66	72
7	7	14	21	28	35	42	49	56	63	70	77	84
8	8	16	24	32	40	48	56	64	72	80	88	96
٩	٩	18	27	36	45	54	63	72	81	90	99	108
10	10	20	30	40	50	60	70	80	90	100	110	120
11	11	22	33	44	55	66	77	88	99	110	121	132
12	12	24	36	48	60	72	84	96	108	120	132	144

Number	1	2	3	4	5	6	7	8	٩	10	11	12
Square	1	4	٩	16	25	36	49	64	81	100	121	132
Cube	1	8	27	64	125	216	343	512	729	1000	1331	1728

#### Multiplying and Dividing by 10, 100 and 1000

10,000	1000	100	10	1 •	1/10	1/100	1/1000

Multiplying x10 digits move left 1 space x100 digits move left 2 spaces x1000 digits move left 3 spaces Dividing +10 digits move right 1 space +100 digits move right 2 spaces +1000 digits move right 3 spaces

#### **MATHEMATICS TABLES – PART 2**



Percentage	Fraction	Decimal		
100%	1	1		
75%	3/4	0.75		
66.6%	2/3	0.66666 recurring		
50%	1/2	0.5		
33.3%	1/3	0.33333 recurring		
25%	1/4	0.25		
20%	1/5 or 2/10	0.2		
12.5%	1/8	0.125		
10%	1/10	0.1		
5%	1/20 or 5/100	0.05		
1%	1/100	0.01		